

NB-1. Question No.I is compulsory

2. Attempt any three from the remaining six questions

3. Figures to the right indicate full marks

Q1a If Laplace transform of $\text{erf}(\sqrt{t}) = \frac{1}{s\sqrt{s+1}}$, then find $L\{e^t \cdot \text{erf}(2\sqrt{t})\}$ [20]

b Find the Orthogonal Trajectory of the family of curves given by $e^{-x} \cdot \cos y + x \cdot y = c$

c Find Complex Form of Fourier Series for e^{2x} ; $0 < x < 2$

d. If the two regression equations are $5x - 6y + 90 = 0$, $15x - 8y - 180 = 0$,

find the means of x and y , the Correlation Coefficient and Standard deviation of x if variance of Y is 1

Q2 Show that the function is Harmonic and find the Harmonic Conjugate $v = e^x \cdot \cos y + x^3 - 3xy^2$ [6]

b Find Laplace Transform of $f(t) = \begin{cases} t & ; 0 < t < 1 \\ 0 & ; 1 < t < 2 \end{cases}$, $f(t+2) = f(t)$ [6]

c. Find Fourier Series expansion of $f(x) = x - x^2$, $-1 < x < 1$ [8]

Q3 a Find the Analytic function $f(z) = u + iv$ if $v = \log(x^2 + y^2) + x - 2y$ [6]

b Find Inverse Z transform of $\frac{3z^2 - 18z + 26}{(z-2)(z-3)(z-4)}$, $3 < |z| < 4$ [6]

c Solve the Differential Equation $\frac{d^2y}{dt^2} + 4y = f(t)$, $f(t) = H(t-2)$, $y(0) = 0$, $y'(0) = 1$ using Laplace Transform [8]

Q4 a Find $Z\{f(k) * g(k)\}$ if $f(k) = \left(\frac{1}{2}\right)^k$, $g(k) = \cos \pi k$ [6]

b Find the Spearman's Rank correlation coefficient between X and Y . [6]

X	60	30	37	30	42	37	55	45
Y	50	25	33	27	40	33	50	42

c Find the inverse Laplace transform of i) $\frac{3s+1}{(s+1)^4}$ ii) $\frac{e^{4-3s}}{(s+4)^{5/2}}$ [8]

Q5 a Find Inverse Laplace Transform using Convolution theorem $\frac{1}{(s-4)^2(s+3)}$

b Show that the functions $f_1(x) = 1$, $f_2(x) = x$ are Orthogonal on $(-1,1)$. Determine the constants a, b such that the function $f(x) = -1 + ax + bx^2$ is Orthogonal to both $f_1(x), f_2(x)$ on the $(-1,1)$

c Find the Laplace transform of i) $e^{-3t} \int_0^t t \sin 4t \, dt$ ii) $\int_0^\infty \frac{e^{-t} - e^{-2t}}{t} dt$

Q6 a Fit a second degree parabola to the given data

X	1	1.5	2	2.5	3	3.5	4
Y	1.1	1.3	1.6	2	2.7	3.4	4.1

b Find the image of $\left|z - \frac{5}{2}\right| = \frac{1}{2}$ under the transformation $w = \frac{3-z}{z-2}$

c Find Half Range Cosine Series for $f(x) = x \sin x$ in $(0, \pi)$ and hence find $\frac{1}{1.3} - \frac{1}{3.5} + \frac{1}{5.7} - \dots = \frac{\pi-2}{4}$

Sem-III - choice based -

Duration: - 3 Hours

Marks: 80 Marks

NB: - Question 1 is compulsory

Solve any three questions from the remaining.

- 1
 - a) Convert decimal number 576.24 into binary, base-9, octal, hexadecimal system. 04
 - b) Construct hamming code for 1010 using odd parity. 04
 - c) Convert $(-89)_{10}$ to its equivalent Sign Magnitude, 1's Complement and 2's Complement Form 04
 - d) Perform $(BC5)_H - (A2B)_H$ without converting to any other base 04
 - e) Prove De Morgans theorem 04
- 2a. Given the logic expression: $A + \overline{B}C + AB\overline{D} + ABCD$ 10
 1. Express it in standard SOP form.
 - 2). Draw K-map and simplify.
 - 3). Draw logic diagram using NOR gates only.
- 2b. Reduce using Quine McClusky method & realize the operation using only NAND gates. 10

$$F(A,B,C,D) = \prod M(0, 2, 3, 6, 7, 8, 9, 12, 13).$$
- 3a. Design a 4-bit binary to gray code converter. 10
- 3b. Design a 4-bit BCD adder using IC 7483 and necessary gates. 10
- 4a. Implement the following logic function using all 4:1 multiplexers with the select inputs as 'B', 'C', 'D', 'E' only. 10

$$F(A,B,C,D,E) = \sum m(0, 1, 2, 3, 6, 8, 9, 10, 13, 15, 17, 20, 24, 30)$$
- 4b. Convert a SR flip flop to J K flip flop 10
- 5a. Design a mod-6 synchronous counter using T FF 10
- 5b. Explain the operation of 4-bit universal shift register. 10
6. Write short notes on any two 20
 - a. VHDL
 - b. TTL and CMOS logic families
 - c. 4-bit Magnitude comparator
 - d. 3 to 8 line decoder

(3 Hours)

[Total Marks: 80]

N.B (1) Question No. 1 is compulsory.

- (2) Solve any **three** questions out of remaining **five** questions.
(3) Assumptions made should be clearly stated.
(4) Figures to the right indicate full marks.

Q.1 (a) Two dice are rolled, find the probability that the sum is
(i) Equal to 1 (ii) Equal to 4 (iii) Less than 13

[6M]

(b) Use the laws of logic to show that
 $[(p \rightarrow q) \wedge \sim q] \rightarrow \sim p$ is a tautology

[6M]

(c) Determine the matrix of the partial order of divisibility on the set A. Draw the Hasse diagram of the Poset. Indicate those which are chains

[8M]

(1) $A = \{1, 2, 3, 5, 6, 10, 15, 30\}$

(2) $A = \{3, 6, 12, 36, 72\}$

Q.2 (a) Find the complement of each element in D_{42} .

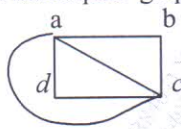
[6M]

(b) Let Q be the set of positive rational numbers which can be expressed in the form $2^a 3^b$, where a and b are integers. Prove that algebraic structure (Q, \cdot) is a group. Where \cdot is multiplication operation.

[6M]

(c) Define isomorphic graphs. Show whether the following graphs are isomorphic or not.

[8M]



G1

Fig (a)

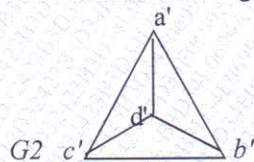
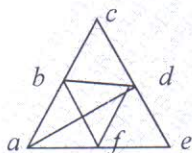


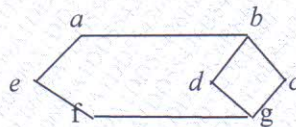
Fig (b)

Q.3 (a) Determine which of the following graph contains an Eulerian or Hamiltonian circuit.

[6M]



Fig(a)



Fig(b)

(b) For all sets A, X and Y show that

$$A \times (X \cap Y) = (A \times X) \cap (A \times Y)$$

[6M]

(c) Let $f(x) = x+2$, $g(x) = x-2$ and $h(x) = 3x$ for $x \in \mathbb{R}$, Where \mathbb{R} = Set of real numbers. Find
 $(g \circ f)$, $(f \circ g)$, $(f \circ f)$, $(g \circ g)$, $(f \circ h)$, $(h \circ g)$, $(h \circ f)$, $(f \circ h \circ g)$

[8M]

Q.4 (a) Let R is a binary relation. Let $S = \{(a, b) \mid (a, c) \in R \text{ and } (c, b) \in R \text{ for some } c\}$ Show that if R is an equivalence relation then S is also an equivalence relation.

[6M]

[TURN OVER]

- (b) Determine the generating function of the numeric function a_r , where [6M]

$$\begin{aligned} \text{(i)} \quad a_r &= 3^r + 4^{r+1}, r \geq 0 \\ \text{(ii)} \quad a_r &= 5, r \geq 0 \end{aligned}$$

- (c) Consider the $(3, 6)$ encoding function $e: B^3 \rightarrow B^6$ defined by [8M]

$$e(000) = 000000 \quad e(001) = 001100 \quad e(010) = 010011 \quad e(011) = 011111$$

$$e(100) = 100101 \quad e(101) = 101001 \quad e(110) = 110110 \quad e(111) = 111010$$

Decode the following words relative to a maximum likelihood decoding function.

- (i) 000101 (ii) 010101

- Q.5 (a) Determine the number of positive integers n where $1 \leq n \leq 100$ and n is not divisible by 2, 3 or 5. [6M]

- (b) Use mathematical induction to show that $1+5+9+\dots+(4n-3) = n(2n-1)$ [6M]

- (c) Find the greatest lower bound and least upper bound of the set $\{3, 9, 12\}$ and $\{1, 2, 4, 5, 10\}$ if they exist in the poset $(\mathbb{Z}^+, /)$. Where $/$ is the relation of divisibility. [8M]

- Q.6 (a) Let $A = \{1, 2, 3, 4\}$ and Let $R = \{(1,1) (1,2) (1,4) (2,4) (3,1) (3,2) (4,2) (4,3) (4,4)\}$. Find transitive closure by Warshall's algorithm. [6M]

- (b) Let $H = \{[0]_6, [3]_6\}$ find the left and right cosets in group Z_6 . Is H a normal subgroup of group of Z_6 . [6M]

- (c) Find the complete solution of the recurrence relation $a_n + 2a_{n-1} = n + 3$ for $n \geq 1$ and with $a_0 = 3$ [8M]

Duration: 3 Hours

Total Marks: 80

- N.B:
- (1) Question No. 1 is Compulsory
 - (2) Attempt any **three** questions of the remaining **five** questions
 - (3) **Figures to the right indicate full marks**
 - (4) Make suitable assumptions wherever necessary with proper justifications

1. (a) What are various operations possible on data structures? (05)
 (b) What are different ways of representing a Graph data structure on a computer? (05)
 (c) Describe Tries with an example. (05)
 (d) Write a function in C to implement binary search. (05)
2. (a) Use stack data structure to check well-formedness of parentheses in an algebraic expression. Write C program for the same. (10)
 (b) Given the frequency for the following symbols, compute the Huffman code for each symbol. (10)

Symbol	A	B	C	D	E
Frequency	24	12	10	8	8

3. (a) Write a C program to implement priority queue using arrays. The program should perform the following operations: (12)
 - i. Inserting in a priority queue
 - ii. Deletion from a queue
 - iii. Displaying contents of the queue
- (b) What are expression trees? What are its advantages? Derive the expression tree for the following algebraic expression: $(a + (b/c)) * ((d/e) - f)$ (08)
4. (a) Write a C program to represent and add two polynomials using linked list. (12)
 (b) How does the Quicksort technique work? Give C function for the same. (08)
5. (a) What is a doubly linked list? Give C representation for the same. (05)
 (b) Given the postorder and inorder traversal of a binary tree, construct the original tree:
 Postorder: D E F B G L J K H C A
 Inorder: D B F E A G C L J H K (10)
 (c) What is hashing? What properties should a good hash function demonstrate? (05)
6. (a) Given an array $\text{int } a[] = \{69, 78, 63, 98, 67, 75, 66, 90, 81\}$. Calculate address of $a[5]$ if base address is 1600. (02)
 (b) Give C function for Breadth First Search Traversal of a graph. Explain the code with an example. (10)
 (c) Write a C program to implement a singly linked list. The program should be able to perform the following operations: (08)
 - (i) Insert a node at the end of the list
 - (ii) Deleting a particular element
 - (iii) Display the linked list

Sem-III - choice Based

Q. P. Code : 26300

(3 Hours)

(Total Marks: 80)

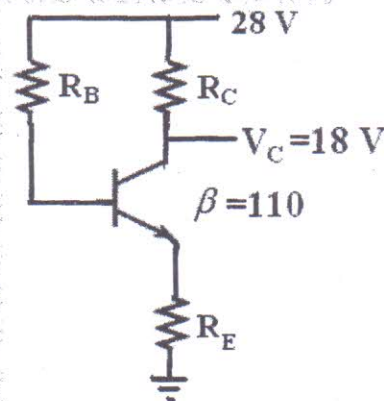
- N.B. :** 1. Question **ONE** is compulsory.
2. Solve any **THREE** out of remaining questions.
3. Draw neat and clean diagrams.
4. Assume suitable data if required.

- Q. 1. A. Explain the concept and significance of CMRR and Slew Rate in case of op-amps. **5**
B. Given $\beta=120$ and $I_E=3.2$ mA for a common-emitter configuration with $r_0=\infty \Omega$, determine:
(a) Z_i
(b) A_v if a load of $2 \text{ k}\Omega$ is applied.
(c) A_i with the $2 \text{ k}\Omega$ load. **5**
C. Discuss the factors that influence modulation index of an FM wave. **5**
D. Justify that adaptive delta modulation superior to delta modulation. **5**

- Q. 2 A. The emitter bias configuration as shown in following figure has the specifications:

$$I_{CQ} = \frac{1}{2} I_{Csat} \quad I_{Csat} = 8 \text{ mA} \quad V_C = 18 \text{ V} \quad \text{and} \quad \beta = 110$$

Determine R_C , R_E and R_B . **10**



- B. Explain how op-am can be used comparator and zero crossing detector. **10**

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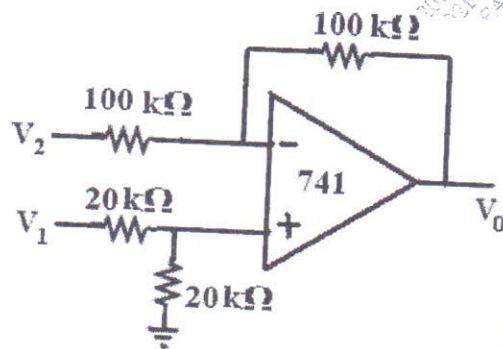
- Q. 3 A. What is the source of the leakage current in a transistor?

If the emitter current of a transistor is 8 mA and I_B is $1/100$ of I_C , determine the levels of I_C and I_B .

- B. Draw and explain Colpitts oscillator.

- C. Explain principle of FDM.

- D. Determine the output voltage for the circuit if $V_1=5V$, and $V_2=3V$



- Q. 4 A. What is DSBSC wave and explain its generation using balanced modulator.

- B. What is multiplexing in communication system? Draw block diagram of TDM-PCM system and explain.

- Q. 5 A. State Shannon's theorem on channel capacity.

What is the maximum capacity of a perfectly noiseless channel whose bandwidth is 120 Hz, in which the values of the data transmitted may be indicated by any one of the 10 different amplitudes?

- B. With respect to neat diagram explain the elements of analog communication system.

- Q. 6 A. What is meant by Nyquist rate in sampling and explain its significance.

- B. Give the proper definition for entropy and information rate.

- C. Write short note on op-amp as differentiator.

- D. Differentiate between Class A and Class C power amplifiers with respect to circuit diagram, operating cycle and power efficiency.