

## Applied Mathematics IV

Duration: 3 hours

Max. Marks 80

N. B.: 1. Question No. 1 is Compulsory.

2. Attempt any 3 Questions from Question no. 2 to 6.

3. Figures to the right indicate the full Marks.

4. Statistical tables are allowed.

- Que. 1 a If  $\lambda$  is an eigen value of nonsingular matrix A then prove that  $\frac{|A|}{\lambda}$  is an eigen value of  $\text{adj } A$ . 5
- b If the random variable X takes the values 1, 2, 3, 4 such that  $2P(X=1)=3P(X=2)=P(X=3)=5P(X=4)$ , find the probability distribution and cumulative distribution of X. 5
- c Find a basis for the orthogonal complement of the subspace in  $R^3$  spanned by the vectors  $V_1 = (1, -1, 3)$ ,  $V_2 = (5, -4, -4)$ ,  $V_3 = (7, -6, 2)$ . 5
- d Evaluate the complex line Integral  $\oint_C \log z \, dz$  where C is the unit circle  $|z|=1$ . 5
- Que.2. a If  $A = \begin{bmatrix} 2 & 3 & 4 \\ 0 & 4 & 2 \\ 0 & 0 & 3 \end{bmatrix}$  find eigen values and eigen vectors of  $A^2 - 2A + I$ . 6
- b Seven dice are thrown 729 times. How many times do you expect at least 4 dice to show 3 or 5? 6
- c Find all Taylor and Laurent series expansions for  $f(z) = \frac{z}{(z-3)(z-4)}$  about  $z=1$  indicating the region of convergence. 8
- Que.3. a A box contains  $2^n$  tickets, among which  ${}^nC_i$  tickets bear the number  $i$ ;  $i=0, 1, 2, \dots, n$ . A group of  $m$  tickets are drawn. What is the expectation of their numbers. 6
- b Verify Cayley-Hamilton theorem for  $A = \begin{bmatrix} 3 & 2 & -1 \\ 0 & 2 & 0 \\ 1 & 1 & 2 \end{bmatrix}$  and hence find  $A^{-1}$ . 6
- c Obtain the equations of the lines of regression for the following data. Also obtain the estimate of X for  $Y=70$ . 8
- |   |    |    |    |    |    |    |    |    |
|---|----|----|----|----|----|----|----|----|
| X | 65 | 66 | 67 | 67 | 68 | 69 | 70 | 72 |
| Y | 67 | 68 | 65 | 68 | 72 | 72 | 69 | 71 |



- Que.4. a Evaluate  $\oint_C \frac{z-1}{(z+1)^2(z-2)} dz$  where  $C$  is  $|z|=3$  6
- b Construct an orthonormal basis of  $R^3$  using Gram Schmidt process to  $S=\{(3, 0, 4), (-1, 0, 7), (2, 9, 11)\}$  6
- c Determine whether the matrix  $A = \begin{bmatrix} 8 & -8 & -2 \\ 4 & -3 & -2 \\ 3 & -4 & 1 \end{bmatrix}$  is diagonalizable, if yes diagonalise it. 8
- Que.5 a Show that the matrix  $A = \begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$  is derogatory and find the minimal polynomial of the matrix. 6
- b A random variable  $X$  has probability density function  $\frac{1}{2^x}$ ,  $x=1,2,3,\dots$  Find moment generating function and hence find mean and variance of  $X$ . 6
- c Of a group of men 5% are under 60 inches height and 40% are between 60 and 65 inches. Assuming a normal distribution find the mean height and standard deviation. 8
- Que.6. a If  $A = \frac{1}{2} \begin{bmatrix} 3 & 1 \\ 1 & 3 \end{bmatrix}$  find  $e^A$  and  $4^A$  6
- b Between 2 pm and 4 pm, the average number of phone calls per minute coming into a switchboard of a company is 2.5. Find the probability that during one particular minute there will be (i) no phone call at all, (ii) at least 5 calls. 6
- c By using Cauchy residue theorem, evaluate 8
- i.  $\int_0^\infty \frac{dx}{x^2+4}$  ii.  $\int_0^{2\pi} \frac{1}{5-4\cos\theta} d\theta$

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# sem-III (choice based) / INST / Transducers - II / M-18

Q.P. Code : 38555

Duration: 3 Hours

Total Marks : 80

Note:

1. Question one is compulsory.
2. Attempt any three from remaining five questions
3. Assume suitable data wherever necessary.

- Q1. Attempt any four** **20**
- a. State Piezo-resistive effect and piezo electric effect.
  - b. Explain the principle of strain gauge and derive gauge factor =  $1 + 2 \nu$ .
  - c. In a rotameter the density of a float is always less than that of flowing fluid. State true or false and justify your answer.
  - d. Compare orifice and venturi meter.
  - e. Draw and explain pressure measurement scheme using bourdon tube and LVDT.
- Q2. a** Explain different arrangements of strain gauges for better sensitivity and temperature compensation. **10**
- Q2. b** A strain gauge is bonded to a beam 0.1 m long and has a cross sectional area  $4 \text{ cm}^2$ . Young's modulus for steel is  $207 \text{ GN/m}^2$ . The strain gauge has an unstrained resistance of 240 ohm and a gauge factor of 2.2. When a load is applied, the resistance of gauge changes by 0.013 ohm. Solve the change in length of the steel beam and the force applied to the beam. **10**
- Q3.a** Describe the following transducers in detail. **10**
- (i) Bellows (ii) Bourdon tube (iii) Dead weight tester
- Q3.b.** Describe working of different types of manometer with advantages and limitations of each type. **10**
- Q4.a.** State basic principle and explain McLeod gauge. **10**
- Q4.b.** What are the steps in calibration of pH meter? Explain pH measurement setup. **10**
- Q5.a.** Derive Bernoulli's equation. **10**
- Q5.b.** A venturi tube of throat diameter 60 mm is placed in a water pipe of diameter 100 mm to measure the volumetric flow. The volumetric flow rate through the tube is  $0.08 \text{ m}^3/\text{s}$  and the water has a density of  $10^3 \text{ kg/m}^3$  and viscosity of  $10^{-3} \text{ Ns/m}^2$ . **10**



- i) Determine the Reynold's number for these conditions.
- ii) The coefficient of discharge is 0.99. Determine the upstream-to-throat differential pressure.

**Q6.** Write short notes (any two):

- Radiation and ultrasonic densitometers
- MEMS
- Optical fiber sensor
- Viscosity measurement

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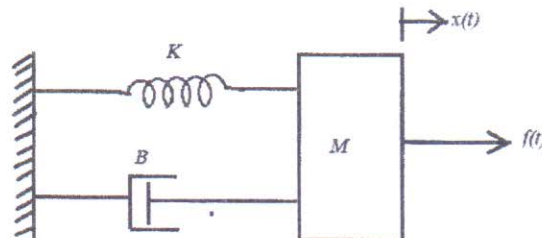
Instructions:

- Q1 is compulsory
- Answer any Three out of remaining Five questions
- Assumptions made should be clearly stated
- Assume any suitable data wherever required but justify the same
- Figure to the right indicate gets full marks
- Illustrate answers with sketches wherever required

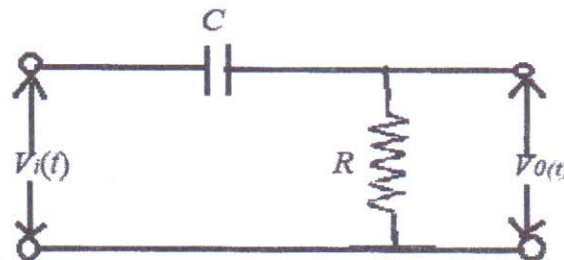
Q1. Answer the following.

(20)

- Discuss how are feedback control systems are classified based on – method of analysis and design, on parameter, type of signals, application, number of input/output, number of open-loop poles of the system, order of the system and damping.
- Obtain the differential equations governing the mechanical system shown in following figure. Find transfer function  $X(s)/F(s)$ .



- Explain the transient and steady – state response. Draw these responses for first and second – order systems.
- Obtain the time response of the following electrical network.



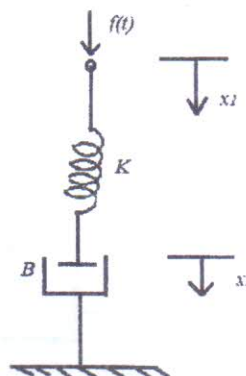
Assume  $C = 1F$ , and  $R = 2\Omega$

Q2. (a) Define open-loop and closed-loop systems and differentiate between them.

(05)

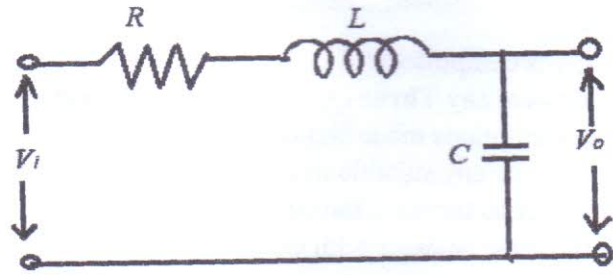
(b) What is meant by analogous systems? Obtain the electrical analogous of following mechanical system using F-V analogy.

(05)

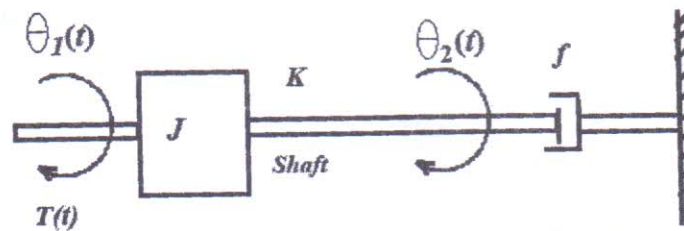




(c) Find the transfer function of the network shown in following Figure using Mason's gain formula.



- Q3. (a) Explain the correlation between time and frequency response specifications.  
 (b) Test the stability of the system represented by following characteristic equation.  
 $s^5 + s^4 + 3s^3 + 9s^2 + 16s + 10 = 0$   
 (c) Write torque equations of the following rotational mechanical system. Obtain the analogous electrical circuit based on Torque-Current and Torque-Voltage analogies.



- Q4. (a) Sketch the root-locus of the unity feedback system having

$$G(s) = \frac{k}{s(s+2)(s+4)}, \text{ where } k \text{ is varied from } -\infty \text{ to } +\infty.$$

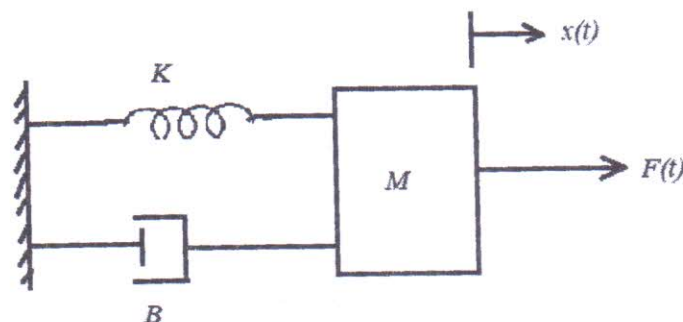
Hence obtain the value of  $k$  for which the system is stable.

- (b) Determine the position, velocity and acceleration constant of the following feedback control systems for which the open-loop transfer functions are –

i)  $G(s) = \frac{20}{(0.5s+1)(s+10)}$

ii)  $G(s) = \frac{K}{s(s+5)(s+20)}$

- Q5. (a) For the system shown in following Figure –



Find i) Transfer function, ii) Damping factor, ii) Natural frequency, iii) Percent overshoot, iv) Peak time, Assume:  $K = 33 \text{ N/m}$ ,  $B = 15 \text{ N-s/m}$ ,  $M = 35 \text{ kg}$



Please check whether you have the right question paper.

- N.B.: 1) Question number 1 is compulsory.  
2) Attempt any three questions from the remaining.  
3) Figures to the right indicate full marks.

1. Answer the following: - [20]
  - (a) Explain the block diagram of Analytical Instrument.
  - (b) Comment on Resolution of Mass Spectrometer.
  - (c) Explain in brief the principle of paramagnetic oxygen analyser.
  - (d) Explain the terms: (i) Chemical Shift (ii) Chromatograph & Chromatogram.
2. (a) State Beer – Lambert Law. Prove that  $A = abc$ . [10]  
(b) Explain the instrument of NMR with the aid of a neat sketch. [10]
3. (a) With neat schematic diagram, explain the working of GM Counter. [10]  
(b) With a diagram, explain the Atomic absorption spectroscopy. [10]
4. (a) What is Half Life Period? [10]  
If the half life period of 100 grams of a radioactive isotope is 8 years, how many grams will remain in 32 years?  
(b) List the parts of GC. Draw and explain the working of Gas chromatograph. [10]
5. (a) Explain the phenomenon of Raman and Rayleigh scattering. [10]  
With neat block diagram, Explain laser based of Raman Spectrometer.  
(b) Explain Time of Flight Mass Spectrometer with neat diagram. [10]
6. Write Short Note on: - [20]
  - (a) Difference between Packed Column and Tubular Column.
  - (b) Photomultiplier tube
  - (c) Single beam Filter Fluorimeter.
  - (d) Difference between Filters and Monochromators.



may 2018

**S.E. (Inst) SEM IV (Choice Base)**  
**Signal Conditioning Circuit Design.**

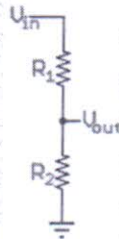
Q. P. Code: 37823

Time: 3 Hours

Total Marks: 80

- N. B. 1) Question No. 1 is compulsory (Any Four).  
 2) Answer any 3 questions from the remaining 5 questions.  
 3) Assume suitable data wherever necessary.

- Q1 (a) Write a short note on zero crossing detector. 20  
 (b) Describe the term loading effect with suitable example.  
 (c) The resistors in a bridge are given by  $R_1=R_2=R_3=120\ \Omega$  and  $R_4=121\ \Omega$ . If the supply voltage is 10V. Find the offset voltage.  
 (d) Draw and explain Sample and Hold circuit.  
 (e) Design a  $\pm 12V$  power supply using IC 78xx.
- Q2 (a) Define multivibrator? Explain astable multivibrator using IC 555 and also design astable multivibrator for 50% duty cycle. 20  
 (b) Draw and explain circuit for ideal integrator with waveforms. Discuss the problems associated with ideal integrator and draw the circuit diagram for practical integrator.
- Q3 (a) A thermistor is to monitor room temperature. It has a resistance of  $3.5\ K\Omega$  at  $20^\circ C$  with a slope of  $-10\%/^\circ C$ . The dissipation constant is  $P_D=5\ mW/^\circ C$ . It is proposed to use the thermistor in the divider as shown below to provide a voltage of 5.0V at  $20^\circ C$ . Evaluate the effect of self-heating. ( $R_2$ = Thermistor;  $R_1=3.5\ K\Omega$ ) 20



- (b) Draw and explain the principle and construction of metal strain gauges. What is the signal conditioning associated with it.
- Q4 (a) Explain successive approximation analog to digital converter. Find ADC output for a 4-bit converter to a 2.87V input, if the reference is 5V. 20  
 (b) Design a second order high pass filter for cutoff frequency equal to 1.5 KHz.
- Q5 (a) A potentiometric displacement sensor is to be used to measure work-piece motion from 0 to 10 cm. The resistance changes linearly over this range from 0 to  $1\ K\Omega$ . Develop signal conditioning to provide a linear, 0- to 10-V output. 20  
 (b) Explain the absolute value circuit with labelled circuit diagram and its waveform.
- Q6 (a) Draw and explain the principle and construction of RTD. What is the signal conditioning associated with it. 10  
 (b) Phase Locked loop 5  
 (c) SMPS 5

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